

الاسم:  
الرقم:

مسابقة في مادة الرياضيات  
المدة: ساعتان

عدد المسائل: خمس

إرشادات عامة: - يسمح باستعمال آلة حاسبة غير قابلة للبرمجة أو اختزان المعلومات أو رسم البيانات.  
- يستطيع المرشح الإجابة بالترتيب الذي يناسبه دون الالتزام بترتيب المسائل الواردة في المسابقة.

### I - (3 points)

In the table below, only one of the proposed answers to each question is correct.

Write down the number of the question and give, **with justification**, its corresponding answer.

N°	Questions	Proposed answers		
		a	b	c
1	$\frac{1}{3} - \frac{1}{3} \times \frac{6}{7} =$	0	$\frac{1}{21}$	$\frac{6}{7}$
2	$(3 + \sqrt{5})^2 - 14 =$	$9 + \sqrt{5}$	0	$6\sqrt{5}$
3	The five grades of a student over 20 are: 10 ; 12 ; 13 ; 16 and 19. The average grade is:	13	14	14.5

### II - (5.5 points)

Given  $A(x) = (3x - 2)^2 - (2x - 1)(3x - 2)$  and  $B(x) = 9x^2 - 4$ .

1) a. Verify that  $A(x) = (3x - 2)(x - 1)$ .

b. Solve the equation  $A(x) = 0$ .

2) Factorize  $B(x)$ .

3) Let  $F(x) = \frac{(3x - 2)(3x + 2)}{A(x)}$ .

a. For what values of  $x$ , is  $F(x)$  defined?

b. Simplify  $F(x)$ .

c. Does the equation  $F(x) = -12$  admit a solution? Justify.

### III - (5.5 points)

1) Solve the following system: 
$$\begin{cases} 2x + 5y = 50\,000 \\ 2x + 3y = 38\,000 \end{cases}$$

2) In a museum, 2 adults and 5 kids buy tickets and pay 50 000 LL;  
4 adults and 6 kids pay 76 000 LL.

a. Prove that the previous information is modeled by the system given in question 1).

b. Find the price of the ticket of an adult and that of a kid.

3) For a group of 30 kids and 4 adults, the director of the museum decided to offer a reduction of 25% on the total amount paid for the tickets. Calculate then the amount paid.

**IV - (4 points)**

Consider the numbers  $\mathbf{A} = (\mathbf{x} + \mathbf{1})^2 + \mathbf{y}^2$  and  $\mathbf{B} = 2(\mathbf{x} - \mathbf{1})^2 + 2(\mathbf{y} - \mathbf{4})^2$  ( $\mathbf{x}$  and  $\mathbf{y}$  are two real numbers).

In what follows take  $\mathbf{x} = \mathbf{4}$  and  $\mathbf{y} = \mathbf{0}$

1) **a.** Calculate A and B.

**b.** verify that  $\mathbf{B} = 2\mathbf{A}$ .

2) Let  $\mathbf{C} = \frac{\mathbf{A}}{\mathbf{B}}$ . Calculate C.

3) Let  $\mathbf{D} = \frac{\sqrt{2} + \sqrt{18}}{2\sqrt{2}}$ .

Verify that D is an integer,

4) Prove that  $\mathbf{C} \times \mathbf{D} = 1$ .

**V- (2 points)**

Consider the numbers  $\mathbf{a} = 6$ ,  $\mathbf{b} = 4$ ,  $\mathbf{c} = 2\sqrt{13}$  and  $\mathbf{d} = \frac{16}{\sqrt{13}}$ .

1) Prove that  $\mathbf{a}^2 + \mathbf{b}^2 = \mathbf{c}^2$ .

2) Prove that  $\mathbf{c} = \frac{32}{\mathbf{d}}$ .