| الاورة العاديةّ للعام | امتحانـات الثشهادة الثُانويـة العامة الفرع : علوم الحياة | وزارة التربيةّ والتعليم العالثي المديرية العامـة للتربية دائرة الامتحانـات |
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| الرقم: الاسم: | مسابقة في مـادة الفيزياء المدة ساعتان |  |

## This exam is formed of three exercises in four pages. <br> The use of non-programmable calculators is recommended.

## First exercise (7 points) Horizontal oscillator

Consider a mechanical oscillator that is formed of a spring (R) of stiffness $k$ and a body (C), of mass $m$ and of center of mass $G$.

## A- Determination of $\mathbf{k}$ and $\mathbf{m}$.

In order to determine the values of $m$ and $k$ of this oscillator, we place it on a horizontal air table. The table functioning normally, we shift (C) from its equilibrium position and we then release it from rest at the instant $\mathrm{t}_{0}=0$. (C) may move then without friction on the table, G moving along a horizontal axis. The origin O of this axis is the position of G when (C) is at equilibrium. x and v are respectively the abscissa and the algebraic


Fig. 1

b) The initial values $\mathrm{x}_{0}$ and $\mathrm{v}_{0}$ of the motion;
c) The value of the proper period $\mathrm{T}_{0}$ of the motion.
2) a) The figure 3 shows the variations of an energy $E$ of the oscillator as a function of time. What form of energy is it? Justify.
b) The energy $E$ is one of two terms of the mechanical energy M.E of the system (body, spring). Redraw figure 3 and show on it the shape of the variations of the mechanical energy M.E and that of the other form of that energy.
3) Deduce the values of $m$ and $k$.

## $B$ - Driving the oscillations

The air table does not function normally any more and the forces of friction can no longer be neglected. We repeat the experiment under the same initial conditions. The variations of x , as a function of time, are recorded by an apparatus thus giving the graph of figure 4.
 measure of the velocity of $G$ at the instant $t$. Convenient equipments allow us to record the variations of $x$ and $v$ and on of the energies of the oscillator as a function of time. These variations are represented in the graphs of the figures1, 2 and 3 . The horizontal plane containing G is taken as a gravitational potential energy reference Take: $\pi^{2}=10$.

1) Referring to the graphs 1 and 2 , determine:
a) The mode of the oscillations;

Fig. 2


Fig. 4

1) Specify the mode of oscillations performed by the oscillator.
2) Determine the value of the variation of the mechanical energy of the oscillator between the Instants: $\mathrm{t}_{0}=0$ and $\mathrm{t}=11 \mathrm{~s}$.
3) A convenient apparatus allows us to drive these oscillations.
a) What does the term «driving » the oscillations represent?
b) Deduce the value of the average power of this apparatus between 0 and 11s.

## Second exercise (7 points) Role of a capacitor in a circuit

The object of this exercise is to study the role of a capacitor in an electric circuit in two different cases. ( $\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$ )
A- Variation of the current in a circuit
1- Qualitative study
We connect the two circuits whose diagrams are represented in the diagram below; the two identical lamps $\mathrm{L}_{1}$ and $\mathrm{L}_{2}$ are fed respectively with two identical generators $\mathrm{G}_{1}$ and $\mathrm{G}_{2}$ each of constant voltage $E$, the component ( D ) being a capacitor that is initially uncharged (Fig.1).


Figure 1


We close the two switches simultaneously at the instant $\mathrm{t}_{0}=0$. We notice initially that $\mathrm{L}_{1}$ and $\mathrm{L}_{2}$ glow with the same brightness, but the brightness of the lamp $\mathrm{L}_{2}$ decreases progressively and finally its light goes out, $\mathrm{L}_{1}$ keeping its same brightness.
a) What can we say about the voltage across each of the lamps at the instant $t_{0}=0$ ? Justify.
b) i) How does the voltage across $L_{2}$ vary starting from the instant $t_{0}=0$ ?
ii) Deduce, when the light of $L_{2}$ goes out, the value of the voltage across the capacitor.

## 2- Quantitative study

We connect a series circuit formed of a resistor of resistance R, a capacitor of capacitance C and a switch K across an ideal generator of e.m.f. E . At the instant $\mathrm{t}_{0}=0$, the capacitor being uncharged, we close the switch K (Fig.2).
At the instant $t$, the charge of the armature $B$ of the capacitor is q and the current carried by the circuit is i .
$\boldsymbol{a}$. Write the relation between i and $\frac{\mathrm{dq}}{\mathrm{dt}}$.


Figure 2
b. Derive the differential equation in $\mathrm{u}_{\mathrm{BM}}=\mathrm{u}_{\mathrm{C}}$.
$\boldsymbol{c}$. This differential equation has as solution: $u_{C}=E\left(1-e^{-\frac{t}{\tau}}\right)$
i) Determine the expression of $\tau$ in terms of R and C .
ii) Determine the expression of the current $i$ in the circuit as a function of time.
iii) Draw the shape of each curve representing the variations of $u_{C}$ and of $i$ as a function of time.
3-Deduce the role of the capacitor in the variation of the current in an RC circuit fed by a DC voltage during the charging phase.

## B- Energy stored in a capacitor 1- Qualitative study

Consider the experiment whose diagram is represented in figure (3), where (M) is a motor to which an body of mass $m$ is suspended, a capacitor of large capacitance, G an ideal generator of constant voltage E, and $\mathrm{K}_{1}$ and $\mathrm{K}_{2}$ are two switches.


Figure 3

In the first step of the experiment, we open $\mathrm{K}_{2}$, and we close $\mathrm{K}_{1}$.
In the second step of the experiment, we open $\mathrm{K}_{1}$ and we close $\mathrm{K}_{2}$. We observe that the body rises.
Explain what happens in each step of the experiment. a tell why the body rises

## 2- Quantitative study

The capacitor has a capacitance $C=1 \mathrm{~F}$, the body has a mass $\mathrm{m}=500 \mathrm{~g}$ and the e.m.f of the generator is $\mathrm{E}=3 \mathrm{~V}$.
$\boldsymbol{a}$ - Calculate the energy initially stored in the capacitor.
b- Calculate the height rised by the body neglecting all energy losses.
c- What type of energy transfer did take place?
$\boldsymbol{d}$ - In fact, the body rises 83 cm . Why?
$e$ - Deduce the role of the capacitor in the previous circuit.

## Third exercise ( 6 points) Determination of the age of the Earth

The object of this exercise is to determine the age of the Earth using the disintegration of a uranium 238 nucleus $\left({ }_{92}^{238} U\right)$ into a lead 206 nucleus $\left({ }_{82}^{206} \mathrm{~Pb}\right)$.


When we determine the number of lead 206 nuclei in a sample taken out from a rock that did not contain lead when it was formed, we can then determine its age that is the same as that of the Earth. The above figure represents the curve of the variation of the number $N_{u}$ of uranium 238 nuclei as a function of time.

1 division on the axis of ordinates corresponds to $10^{12}$ nuclei.
1 division on the axis of abscissa corresponds to $10^{9}$ years.
The equation of the disintegration of Uranium 238 into lead 206 is:
${ }_{92}^{238} \mathrm{U} \rightarrow{ }_{82}^{206} \mathrm{~Pb}+\mathrm{x} \beta^{-}+\mathrm{y} \alpha$
1 .Determine, specifying the laws used, the values of x and y .
2. Referring to the curve, indicate the number $\mathrm{N}_{\mathrm{ou}}$ of uranium 238 nuclei existing in the sample at the date of its birth $t_{0}=0$.
3. Referring to the curve , determine the period (half-life) of uranium 238.Deduce the value of the radioactive constant $\lambda$ of uranium 238.
4. a) Give, in terms of $N_{0 \mathrm{u}}, \lambda$ and t , the expression of the number $\mathrm{N}_{\mathrm{u}}$ of uranium 238 nuclei remaining in
the sample at instant t .
b) Calculate the number of uranium 238 nuclei remaining in the sample at instant $\mathrm{t}_{1}=2 \times 10^{9}$ years:
c) Verify this result graphically:
5. The number of lead 206 nuclei existing in the sample at the instant of measurement (age of the Earth) is $\mathrm{N}_{\mathrm{pb}}=2.5 \times 10^{12}$ nuclei.
a) Give the relation among $N_{u}, N_{0 u}$ and $N_{p b}$.
b) Calculate the number $\mathrm{N}_{\mathrm{u}}$ of uranium nuclei remaining in the sample at the date of measurement.
c) Determine the age of the Earth.

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| الرقم: الاسم: | مسابقة في مادة الفيزياء الددة ساعتان | مشروع معيار التصحيح |


| Part of the $\mathbf{Q}$ | Answer | Mark |
| :---: | :---: | :---: |
|  | First exercise (7 points) |  |
| A.1.a | Mode: free non-damped oscillations | 0.50 |
| A.1.b | At $\mathrm{t}=0$ we have: $\mathrm{x}=\mathrm{x}_{0}=4 \mathrm{~cm}$ and $\mathrm{v}=\mathrm{v}_{0}=0$. | 0.50 |
| A.1.c | $\mathrm{T}_{0}=2 \mathrm{~s}$ | 0.50 |
| A.2.a | Elastic potential energy. Since at $\mathrm{t}=0 \mathrm{x}=\mathrm{X}_{\mathrm{m}}$. And the value of that energy is maximum. | 0.50 |
| A.2.b | The curves are represented in the adjacent figure. | 1.25 |
| A. 3 | $\begin{aligned} & \frac{1}{2} \mathrm{kX}_{\mathrm{m}}^{2}=8 \times 10^{-4} \Rightarrow \mathrm{k}=1 \mathrm{~N} / \mathrm{m} . \\ & \mathrm{T}_{0}=2 \pi \sqrt{\frac{\mathrm{~m}}{\mathrm{k}}} \Rightarrow \mathrm{~m}=\frac{\mathrm{kT}_{0}^{2}}{4 \pi^{2}} \Rightarrow \mathrm{~m}=0.1 \mathrm{~kg} \end{aligned}$ | 1.50 |
| B. 1 | Mode: Free and damped oscillations | 0.50 |
| B. 2 | $\Delta \mathrm{M} . \mathrm{E}=\frac{1}{2} \mathrm{kX}_{\mathrm{m}(\mathrm{t})}^{2}-\frac{1}{2} \mathrm{kX}_{\mathrm{m}(0)}^{2}=-6 \times 10^{-4} \mathrm{~J} .$ | 0.75 |
| B.3.a | Provides energy to compensate for the loss during the oscillations. | 0.25 |
| B.3.b | $\mathrm{P}_{\mathrm{av}}=\frac{\|\Delta \mathrm{M} \cdot \mathrm{E}\|}{\Delta \mathrm{t}}=5.45 \times 10^{-5} \mathrm{~W}$. | 0.75 |
|  | Second exercise (7 points) |  |
| A.1.a | the two voltages are equal because the lamps glow with the same brightness. | 0.25 |
| A.1.b.i | $\mathrm{u}_{2}$ decreases, in fact $\mathrm{E}=\mathrm{u}_{2}+\mathrm{u}_{\mathrm{C}}=$ cte but $\mathrm{u}_{\mathrm{C}}$ increase thus $\mathrm{u}_{2}$ decreases. | 0.50 |
| A.1.b.ii | - When the light of $L_{2}$ goes out $u_{2}=0 \Rightarrow E=u_{C}+u_{2}=u_{C} \Rightarrow$ we can then find the voltage of the generator $\mathrm{G}_{2}$ across the capacitor. | 0.50 |
| A.2.a | $\mathrm{i}=\frac{\mathrm{dq}}{\mathrm{dt}}$ | 0.25 |
| A.2.b | $\mathrm{E}=\mathrm{Ri}+\mathrm{u}_{\mathrm{C}}, \text { but } \mathrm{i}=\frac{\mathrm{dq}}{\mathrm{dt}}=\mathrm{C} \frac{\mathrm{du}_{\mathrm{C}}}{\mathrm{dt}} \Rightarrow \mathrm{E}=\mathrm{RC} \frac{\mathrm{du}_{\mathrm{C}}}{\mathrm{dt}}+\mathrm{u}_{\mathrm{C}} .$ | 0.75 |
| A.2.c.i | $\begin{aligned} & C \frac{d u_{C}}{d t}=C \times \frac{E}{\tau} e^{-\frac{t}{\tau}} \Rightarrow E=R \times C \times \frac{E}{\tau} e^{-\frac{t}{\tau}}+E\left(1-e^{-\frac{t}{\tau}}\right) \\ & \Rightarrow \frac{R C}{\tau}-1=0 \Rightarrow \tau=R C . \end{aligned}$ | 0.75 |


| A.2.c.ii | $\mathrm{i}=\mathrm{C} \frac{\mathrm{du}_{\mathrm{C}}}{\mathrm{dt}}=\mathrm{C} \times \frac{\mathrm{E}}{\tau} \mathrm{e}^{-\frac{\mathrm{t}}{\tau}}=\frac{\mathrm{E}}{\mathrm{R}} \mathrm{e}^{-\frac{\mathrm{t}}{\tau}} .$ | 0.50 |
| :---: | :---: | :---: |
| A.2.c.iii |   | 0.50 |
| A.2.c.iv | The capacitor does not allow the passage of the cuntent except uumb a sumi time when the circuit is fed by a DC voltage. | 0.50 |
| B. 1 | In the first step, the capacitor is charged till it reaches a voltage $u_{C}=E$. In the second step, the capacitor is discharged in the motor by providing across the motor a voltage $u_{C}$ which decreases from the value $E$, thus it allows the lifting of the body. | 0.50 |
| B.2.a | $\mathrm{W}=1 / 2 \mathrm{CE}^{2}=1 / 2(1)(9)=4.5 \mathrm{~J}$. | 0.50 |
| B.2.b | $\mathrm{W}=\mathrm{mgh}_{\max } \Rightarrow \mathrm{h}_{\max }=\frac{4.5}{0.5 \times 10}=0.9 \mathrm{~m} .$ | 0.75 |
| B.2.c | The electric energy stored in the capacitor is transformed into mechanical energy. | 0.25 |
| B.2.d | Because of friction | 0.25 |
| B.2.e | The capacitor stores electric energy and restitute this energy when needed. | 0.25 |
|  | Third exercise (6 points) |  |
| 1 | ${ }_{92}^{238} U \rightarrow{ }_{82}^{206} \mathrm{~Pb}+\mathrm{X}_{-1}^{0} e+y_{2}^{4} \mathrm{He}$ <br> The laws of conservation of the mass number and the charge number give $\begin{aligned} & 238=206+4 y \Rightarrow y=8 \alpha \text { decays. } \\ & 92=82-x+2 y \Rightarrow x=6 \beta \text { decays. } \end{aligned}$ | 1.25 |
| 2 | $\mathrm{N}_{00 \mathrm{ou}}=5 \times 10^{12}$ nuclei | 0.50 |
| 3 | For the half-life $\mathrm{N}_{\mathrm{u}}=\frac{N_{O U}}{2}=2.5 \times 10^{12}$ nuclei. <br> On the graph we find $\mathrm{T} \approx 4.5 \times 10^{9}$ years. <br> The radioactive constant $\lambda=\frac{0.693}{T}=\frac{0.693}{4.5 \times 10^{9}}=1.54 \times 10^{-10}$ year $^{-1}$ | 1.50 |
| 4.a | $\mathrm{N}_{\mathrm{u}}=\mathrm{N}_{\mathrm{ou}} \mathrm{e}^{-7 \mathrm{ta}}$ | 0.25 |
| 4.b | $\mathrm{N}_{\mathrm{u}}=5 \times 10^{12} \mathrm{e}^{-1.54 \times 10^{-10} \times 2 \times 10^{9}}=3.675 \times 10^{12}$ nuclei. | 0.75 |
| 4.c | On the graph: $2 \times 10^{9}$ years corresponds $3.7 \times 10^{12}$ nuclei | 0.50 |
| 5.a | $\mathrm{N}_{\mathrm{ou}}=\mathrm{N}_{\mathrm{u}}+\mathrm{N}_{\mathrm{Pb}}$ | 0.25 |
| 5.b | a. $\quad \mathrm{N}_{\mathrm{u}}=\mathrm{N}_{\mathrm{ou}}-\mathrm{N}_{\mathrm{Pb}}=5 \times 10^{12}-2.5 \times 10^{12}=2.5 \times 10^{12}$ nuclei. | 0.50 |
| 5.c | $\mathrm{N}_{\mathrm{u}}=\frac{N_{O U}}{2}$; the age of the Earth is equal to the half-life of uranium 238. this age is $4.5 \times 10^{9}$ years. | 0.50 |

