


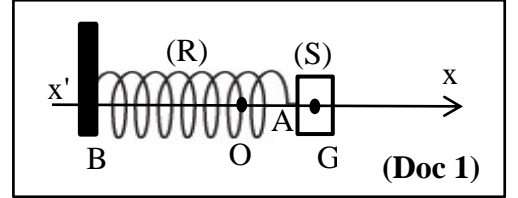
المادة: الفيزياء الشهادة: الثانوية العامة الفرع: العلوم العامة نموذج رقم 2 المدة: ثلاث ساعات	الهيئة الأكاديمية المشتركة قسم: العلوم	 المركز العلمي للبحوث والابتكار
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نموذج مسابقة (يراعي تعليق الدروس والتوصيف المعدل للعام الدراسي 2016-2017 وحتى صدور المناهج المطورة)

This test includes four mandatory exercises. The use of non-programmable calculators is allowed.

### Exercise 1 (6½ points) Oscillations of a horizontal elastic pendulum

An elastic pendulum (R) is formed of a solid (S), of mass  $m$ , attached to the extremity A of a horizontal spring of stiffness  $k = 80 \text{ N/m}$ ; the other extremity B of the spring is attached to a fixed support as shown in the adjacent document (Doc 1).



The center of inertia G of the solid can move along a horizontal axis  $x'x$ .

At equilibrium, the center of inertia G of (S) is confounded with the origin O of the axis  $x'x$ .

We shift the solid from its equilibrium position and then we release it from rest at the instant  $t_0 = 0$ . G starts oscillating on either side of its equilibrium position O.

At an instant  $t$ , the abscissa of G is  $x$  and the algebraic value of its velocity is  $v = \frac{dx}{dt} = x'$ .

The horizontal plane passing through G is the reference level of the gravitational potential energy.

#### 1) Free undamped oscillations

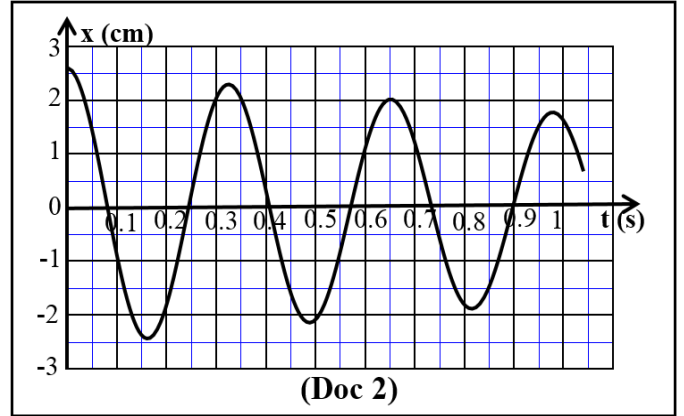
We neglect the force of friction.

- 1-1) Write down, at an instant  $t$ , the expression of the mechanical energy of the system (pendulum -Earth).
- 1-2) Derive the second order differential equation in  $x$  that describes the motion of (S).
- 1-3) Deduce the expression of the proper period  $T_0$  of these oscillations.

#### 2) Free damped oscillations

In reality, the friction force has a certain value. Taking into account the previous initial conditions, a device allows to register the variations of  $x$  as a function of time  $t$  as shown in the adjacent document (Doc 2).

- 2-1) Referring to the graph, determine the pseudo-period  $T$  of the oscillations.
- 2-2) Calculate the average power dissipated between the instants  $t_0 = 0$  and  $t_1 = 3T$ .



#### 3) Forced oscillations

We connect now the extremity B of the spring to a vibrator of adjustable frequency  $f_v$  and of constant amplitude. We give  $f_v$  different values and we register, for every value of  $f_v$ , the corresponding value of the amplitude  $x_m$  of the oscillations of G as shown in the document (Doc 3) below.

(Doc 3)	$f_v$ (Hz)	1.5	2	2.5	2.8	3	3.2	3.3	3.6	4	4.5
	$x_m$ (cm)	0.4	0.6	1	1.5	2.1	2.3	2	1.5	1	0.7

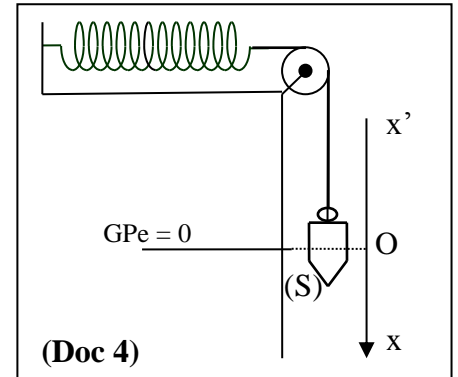
- 3-1) Referring to the table, determine the approximate value of the proper period of the oscillations of (R).
- 3-2) Determine the approximate value of  $m$ .
- 3-3) Sketch the graph giving the variation of  $x_m$  as a function of  $f_v$ .
- 3-4) Trace, with justification, the shape of the previous curve when the force of friction has a greater value.

## Exercise 2 (7½ points)

### Synchronous pendulums

#### 1) Elastic pendulum

A spring, of force constant  $k$  and of negligible mass, is placed on a smooth horizontal table. The left end of the spring is fixed to a support and the right end is connected to the end of a massless string passing over a light pulley as shown in the adjacent document (Doc 4). A particle (S), of mass  $m$ , is tied to the other end of the string. At equilibrium, (S) is at O. Take the horizontal plane passing through O as the reference level of the gravitational potential energy and  $g = 10 \text{ m/s}^2$ . Neglect all resistive forces.



**1-1)** When (S) is at equilibrium, it coincides with the origin O of the vertical axis  $x'ox$ , and the spring is extended by  $\Delta\ell$ .

Show that  $\Delta\ell = \frac{mg}{k}$ .

**1-2)** The particle, pulled down by 4 cm, is released from rest at the instant  $t_0 = 0$ . At an instant  $t$ , the abscissa of the particle is  $x$  and the algebraic value of its velocity is  $v = \frac{dx}{dt} = x'$ .

**1-2-1)** Show that, at an instant  $t$ , the expression of the mechanical energy of the system [(S), Earth, spring, string, pulley] is given by:  $ME = \frac{1}{2}k(\Delta\ell + x)^2 - mgx + \frac{1}{2}mv^2$ .

**1-2-2)** Determine the second order differential equation, in  $x$ , that describes the motion of (S).

**1-2-3)** Deduce the expression of the proper angular frequency  $\omega_0$  of the pendulum and give that of its proper period  $T_0$  in terms of  $\Delta\ell$  and  $g$ .

**1-2-4)** Determine the time equation of the motion of (S) knowing that it is of the form:

$$x = x_m \sin(\omega_0 t + \varphi).$$

#### 2) Simple pendulum

A simple pendulum is formed of an inextensible and massless string of length  $L$  and a particle (S') of mass  $m$  as shown in the adjacent document (Doc 5). Suspended in a proper way, (S') is shifted from its equilibrium position by an angular abscissa  $\theta_0 = 0.10 \text{ rd}$ , and then released from rest at the instant  $t_0 = 0$ . The pendulum performs oscillations of angular amplitude  $\theta_m = 0.10 \text{ rd}$ . At an instant  $t$ , the angular abscissa of the pendulum is  $\theta$  and its angular velocity is  $\theta' = \frac{d\theta}{dt}$ .

Take the horizontal plane passing through the equilibrium position of (S') as the reference level of the gravitational potential energy and  $g = 10 \text{ m/s}^2$ . Neglect all resistive forces.

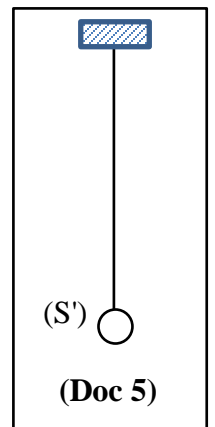
Take whenever needed, for small values of  $\theta$ , ( $\theta$  in rd):  $\cos \theta = 1 - \frac{\theta^2}{2}$  or  $\sin \theta = \theta$ .

**2-1)** Determine, at an instant  $t$ , the expression of the mechanical energy of the system (pendulum-Earth).

**2-2)** Determine the second order differential equation, in  $\theta$ , that describes the motion of the pendulum.

**2-3)** Deduce the expression of the proper angular frequency  $\omega'_0$  of this pendulum and give that of its proper period  $T'_0$  in terms of  $L$  and  $g$ .

**2-4)** Determine the time equation of the motion of the pendulum knowing that it is of the form:  $\theta = \theta_m \sin(\omega'_0 t + \varphi')$ .



#### 3) Comparison

Compare the proper periods  $T_0$  and  $T'_0$  of these pendulums and give the condition to be satisfied by an elastic pendulum and a simple pendulum to be synchronous.

### Exercise 3 (6½ points)

### Sparks in a Car ignition system

The ability of a coil, to oppose rapid changes in current, makes it very useful for spark generation.

The engine of a car requires that the fuel-air mixture in each cylinder must be ignited at proper times. This is achieved by means of a spark plug, which essentially consists of a pair of electrodes separated, at a specific distance, by an air gap. By creating a large voltage (a few tens of thousands of volts) between the electrodes, a spark is formed across the gap, thereby igniting the fuel.

The coil of a car ignition system has an inductance  $L = 20 \text{ mH}$  and a resistance  $r = 2 \ \Omega$ .

The electromotive force of car battery is:  $E = 12 \text{ V}$ .

#### 1) Switch K is closed

The adjacent document (Doc 6) shows the circuit of a spark plug in a car where the resistor used for protection is of resistance  $R = 4 \ \Omega$ .

At the instant  $t_0 = 0$ , the switch K of the circuit is closed.

1-1) The current in the branch of the spark plug is considered zero. Justify.

1-2) At an instant  $t$ , the circuit carries the current  $i$ . Using the law of addition of voltages, determine the differential equation in  $i$ .

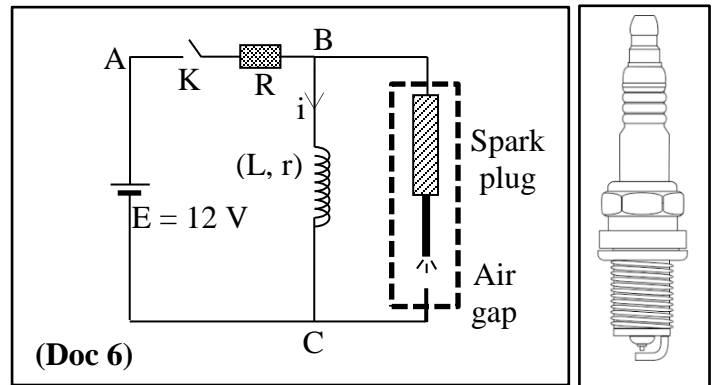
1-3) Deduce, in steady state, the current  $I_0$  carried by the circuit.

1-4) Calculate the time needed by the current  $i$  to reach, practically, its maximum value  $I_0$  knowing that the time constant  $\tau$  of the circuit is:  $\tau = \frac{L}{(R+r)}$ .

1-5) Calculate the maximum magnetic energy stored by the coil.

1-6) Determine, in steady state, the voltage across the air gap of the spark plug.

1-7) A spark is a visible disruptive discharge of electricity between two electrodes of high voltage. It is preceded by an ionization of the gas (air - fuel) then followed by a rapid heating effect that burns the fuel. Specify if sparks are created in the air gap during the growth of the current in the circuit.



#### 2) Switch K is opened

2-1) When the switch K is opened, the current drops to zero during  $1 \ \mu\text{s}$ . Determine the voltage developed across the electrodes of the plug.

2-2) Specify if sparks are produced in the air gap.

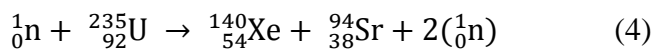
2-3) The sparks in the air gap get weaker as the distance between the electrodes gets larger. Explain why the spark plug must be changed after being used for a long time.

**Exercise 4 (7 points)****Nuclear reactions**


Consider the following four reactions (1), (2), (3) and (4) and the masses of some nuclei.

	${}^1_1\text{H}$	${}^2_1\text{H}$	${}^3_1\text{H}$	${}^4_2\text{He}$	${}^1_0\text{n}$	${}^{235}_{92}\text{U}$	${}^{140}_{54}\text{Xe}$	${}^{94}_{38}\text{Sr}$
m(u)	1.0073	2.0141	3.0155	4.0015	1.0087	235.0439	139.9216	93.9153

$$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg} = 931.5 \text{ MeV}/c^2; \quad c = 3 \times 10^8 \text{ m/s}; \quad 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}.$$

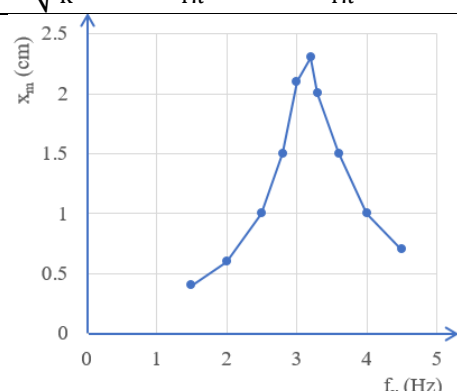


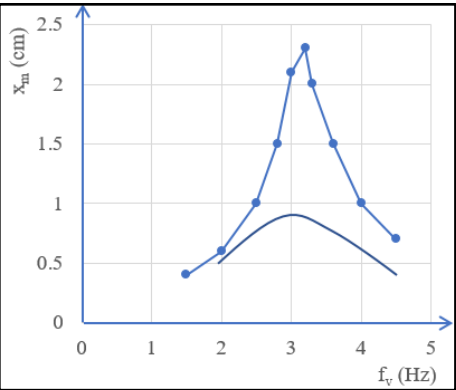
- 1) Give the type of each of these four reactions.
- 2) Consider the reaction (1).
  - 2-1) Calculate A and Z indicating the laws used.
  - 2-2) Name the particle X and give its symbol.
- 3) The deuterium nuclei undergo the nuclear reactions (2) and (3).
  - 3-1) Write the overall reaction (5) that takes place.
  - 3-2) Determine, in MeV and in joule, the energy liberated by this reaction.
- 4) Consider the reaction (4).
  - 4-1) Calculate, in u and in kg, the mass lost.
  - 4-2) Determine the released energy.
  - 4-3) The released energy by the atomic bomb dropped at Hiroshima was estimated to be the equivalent to 15 kilotons of dynamite or  $63 \times 10^{12} \text{ J}$ .
    - 4-3-1) Calculate the number of uranium-235 nuclei that underwent fission in this bomb assuming that all of the fission reactions took place as reaction (4) from the energetic point of view.
    - 4-3-2) Determine the mass of reacting uranium-235 necessary to release this energy.
- 5) The combustion of a mass  $m_1 = 1 \text{ kg}$  of fuel oil liberates an amount of energy  $E = 4.3 \times 10^7 \text{ J}$ .
  - 5-1) Determine the mass  $m_2$  of the deuterium nuclei and the mass  $m_3$  of uranium nuclei that may produce this energy.
  - 5-2) Classify in ascending order the masses  $m_1$ ,  $m_2$  and  $m_3$  and indicate the substance that is preferable to be used to obtain energy, regardless of other factors.

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أسس التصحيح (تراعي تعليق الدروس والتوصيف المعدل للعام الدراسي 2016-2017 وحتى صدور المناهج المطورة)

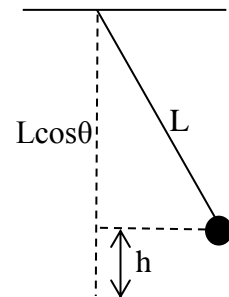
### Exercise 1 (6½ points) Oscillations of a horizontal elastic pendulum

Question	Answer	Mark
1-1	$ME = KE + PE \quad \forall t$ $ME = \frac{1}{2} mv^2 + \frac{1}{2} kx^2$	¼ ¼
1-2	There is no friction, so the mechanical energy of the system is conserved Then $ME = \text{constant} \quad \forall t$ $\frac{dME}{dt} = mvv' + kxx' = 0 \quad \forall t$ $mx' \left( x'' + \frac{k}{m} x \right) = 0 \quad \forall t$ The product of two physical quantities is always nil, but $mx'$ is not always nil, we get: $x'' + \frac{k}{m} x = 0$	½ ½
1-3	The differential equation is of the form $x'' + \omega_0^2 x = 0$ The oscillator undergoes simple harmonic oscillation of proper angular frequency $\omega_0 = \sqrt{\frac{k}{m}}$ the proper period is thus: $T_0 = \frac{2\pi}{\omega_0} = 2\pi \sqrt{\frac{m}{k}}$	¼ ¼
2-1	Using the graph, $3T = 0.98$ then $T = 0.326$ s	½
2-2	for $t_0 = 0$ , $x_0 = 2.6$ cm, $ME_0 = \frac{1}{2} kx_0^2 = 0.02704$ J ( $KE_0 = 0$ because the elongation is maximum); for $t = 3T$ , $x = 1.8$ cm, $ME = \frac{1}{2} kx^2 = 0.01296$ J ( $KE = 0$ because the elongation is maximum); $P_{\text{av diss}} = \frac{\text{Energy lost}}{\text{duration}} = \frac{0.02704 - 0.01296}{0.98} = 0.0144$ W	½ ½
3-1	Referring to the graph, damping is relatively very weak. In this case, the resonant frequency is too close to the proper frequency of the pendulum. $f_0$ corresponds to the highest amplitude, $f_0 = 3.2$ Hz, thus, $T_0 = 1/f_0 = 0.3125$ s	½ ½
3-2	$T_0 = 2\pi \sqrt{\frac{m}{k}}$ ; $m = \frac{T_0^2 \times k}{4\pi^2} = \frac{(0.3125)^2 \times 80}{4\pi^2} = 0.198$ kg	½ ½
3-3		½

3-4	<p>When the force of friction increases, the maximum value of the amplitude of the curve of resonance becomes smaller (the bandwidth larger and the resonance frequency smaller).</p> <p>When the force of friction becomes greater, the phenomenon of resonance disappears, and (S) is then sensitive to a large band of frequencies, the bandwidth becomes larger.</p> <p><i>Remark: The shape of the curve must be in accordance with the initial conditions and in respect for the problem situation.</i></p>		1/2
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**Exercise 2 (7½ points) Synchronous pendulums**

Question	Answer	Mark
1-1	<p>The Particle S is at equilibrium: <math>W = T</math>  <math>mg = k\Delta\ell \Rightarrow \Delta\ell = \frac{mg}{k}</math></p>	1/2 1/2
1-2-1	<p><math>ME = KE + PE_g + PE_e = \frac{1}{2} k(\Delta\ell + x)^2 - mgx + \frac{1}{2} mv^2</math></p>	1/2
1-2-2	<p>There is no friction thus ME is conserved  <math>ME = \frac{1}{2} k\Delta\ell^2 + \frac{1}{2} kx^2 + kx\Delta\ell - mgx + \frac{1}{2} mv^2 = \text{constant} \quad \forall t \quad (k\Delta\ell = mg)</math>  <math>\frac{dME}{dt} = 0 + kxx' + mvv' = 0 \quad \forall t \Rightarrow mx' \left( x'' + \frac{k}{m} x \right) = 0 \quad \forall t</math>            The product of two physical quantities is always nil, but <math>mx'</math> is not always nil,            we get: <math>x'' + \frac{k}{m} x = 0</math></p>	1/2 1/2
1-2-3	<p>The differential equation is of the form <math>x'' + \omega_0^2 x = 0</math>            The oscillator undergoes simple harmonic oscillations of proper angular frequency <math>\omega_0 = \sqrt{\frac{k}{m}}</math>            the proper period is thus: <math>T_0 = 2\pi \sqrt{\frac{m}{k}} T_0 = 2\pi \sqrt{\frac{\Delta\ell}{g}}</math></p>	1/4 1/4
1-2-4	<p><math>\omega_0 = \sqrt{\frac{k}{m}}</math>  <math>x = x_m \sin(\omega_0 t + \varphi); v = x_m \omega_0 \cos(\omega_0 t + \varphi);</math>            at <math>t_0 = 0: x_0 = x_m \sin(\varphi) &gt; 0</math> and <math>v_0 = x_m \omega_0 \cos(\varphi) = 0</math> then <math>\varphi = \frac{\pi}{2}</math> rd  <math>x_0 = x_m = 4</math> cm.  <math>x = 4 \sin\left(\sqrt{\frac{k}{m}} t + \frac{\pi}{2}\right);</math> (t in s and x in cm)</p>	1/4 1/4 1/4
2-1	<p><math>ME = PE_g + KE</math>  <math>ME = mgh + \frac{1}{2} I \theta^2 = mgL(1 - \cos\theta) + \frac{1}{2} I \theta^2</math>            Knowing that <math>\theta = 0.1</math> rd <math>&lt; 6^\circ</math>, <math>\cos\theta = 1 - \frac{\theta^2}{2}</math>  <math>ME = \frac{1}{2} mgL\theta^2 + \frac{1}{2} mL^2 \theta^2</math></p>	1/4 1/4 1/2



2-2	$ME = \frac{1}{2} mgL\theta^2 + \frac{1}{2} mL^2 \dot{\theta}^2 = \text{constant} \quad \forall t$ $\frac{dME}{dt} = 0$ then: $mgL\theta\dot{\theta} + mL^2 \dot{\theta}\ddot{\theta} = 0$ ; $mL\dot{\theta}$ is not always nil $g\theta + L\ddot{\theta} = 0 \Rightarrow \ddot{\theta} + (g/L)\theta = 0$	$\frac{1}{4}$   $\frac{1}{2}$
2-3	The differential equation has the form $\ddot{\theta} + \omega_0'^2\theta = 0$ The oscillator undergoes simple harmonic oscillation of proper angular frequency $\omega_0'$ with $\omega_0'^2 = \frac{g}{L}$ , thus, $\omega_0' = \sqrt{\frac{g}{L}}$ The proper period is thus: $T_0' = \frac{2\pi}{\omega_0'} = 2\pi\sqrt{\frac{L}{g}}$	$\frac{1}{2}$
2-4	$\theta = \theta_m \sin(\omega_0' t + \varphi')$ ; $\dot{\theta} = \theta_m \omega_0' \cos(\omega_0' t + \varphi')$ ; at $t_0 = 0$ : $\theta_0 = \theta_m \sin(\varphi') > 0$ and $\dot{\theta}_0 = \theta_m \omega_0' \cos(\varphi') = 0$ then $\varphi' = \frac{\pi}{2}$ rd $\theta_0 = \theta_m = 0,1$ rd $\theta = 0,1 \sin\left(\sqrt{\frac{g}{L}} t + \frac{\pi}{2}\right)$ ; (t in s and $\theta$ in rd)	$\frac{1}{4}$  $\frac{1}{4}$  $\frac{1}{4}$
3	$T_0 = 2\pi\sqrt{\frac{\Delta\ell}{g}}$ and $T_0' = 2\pi\sqrt{\frac{L}{g}}$ The two pendulums are synchronous, $T_0 = T_0' \Rightarrow \Delta\ell = L$	$\frac{1}{2}$

### Exercise 3 (6½ points)

### Sparks in a Car ignition system

Question	Answer	Mark
1-1	Since the branch of the spark plug is an open circuit due to the air gap	$\frac{1}{2}$
1-2	$u_{AC} = u_{AB} + u_{BC}$ ; $E = Ri + (ri + L di/dt)$ $\frac{E}{L} = \frac{(R+r)}{L} i + \frac{di}{dt}$	$\frac{1}{2}$ $\frac{1}{2}$
1-3	In steady state: $i = I_0 = \text{constant}$ $\frac{E}{L} = \frac{(R+r)}{L} I_0 + \frac{di}{dt}$ , ( $di/dt = 0$ ) $E = (R+r) I_0 \Rightarrow I_0 = E/(R+r) = 12/6 = 2$ A	$\frac{1}{2}$ $\frac{1}{2}$
1-4	$\Delta t = 5\tau = 5\frac{L}{(R+r)} = 5 \times 0,02/6 = 0,0167$ s	$\frac{1}{2}$
1-5	$E_{\text{mag}}(\text{max}) = \frac{1}{2} LI_0^2 = \frac{1}{2} \times 0,02 \times 2^2 = 0,04$ J	$\frac{1}{2}$
1-6	$u_{\text{air gap}} = u_{BC} = rI_0 = 2 \times 2 = 4$ V	$\frac{1}{2}$
1-7	No since $u_{\text{air gap}} = 4$ V is small.	$\frac{1}{2}$
2-1	The average induced e.m.f. is: $e_{\text{av}} = -L(\Delta i/\Delta t) = -0,02 \times (0-2)/10^{-6} = 40000$ V $\Rightarrow  u_{\text{air gap}}  = u_{CB} \approx 40000$ V (since $ri$ is assumed very small).	$\frac{1}{2}$ $\frac{1}{2}$
2-2	Yes, sparks are produced in the gap because the voltage is very high.	$\frac{1}{2}$
2-3	The sparks produced in the air gap will melt gradually the electrodes of the spark plug; this causes an increase in the distance between them and consequently the sparks get fainter and then the plug must be replaced by a new one.	$\frac{1}{2}$

**Exercise 4 (7 points)**
**Nuclear reactions**

Question	Answer	Mark
1	(1): Natural radioactivity (2): and (3): fusion (4): fission	1/4 1/2 1/4
2-1	By applying Soddy's laws: Conservation of the mass number: $235 = 231 + A \Rightarrow A = 4$ Conservation of the charge number: $92 = 90 + Z \Rightarrow Z = 2$	1/4 1/4 1/4
2-2	This particle is the helium-4 nucleus; its symbol is ${}^4_2\text{He}$ .	1/4
3-1	Adding 2 and 3 we obtain: $3 {}^2_1\text{H} + {}^3_1\text{H} \rightarrow {}^4_2\text{He} + {}^3_1\text{H} + {}^1_1\text{H} + {}^1_0\text{n}$ $3 {}^2_1\text{H} \rightarrow {}^4_2\text{He} + {}^1_1\text{H} + {}^1_0\text{n}$ (5)	1/2
3-2	$E_{\text{Lib.}} = \Delta m \cdot c^2 = [(3 \times 2.0141) - (4.0015 + 1.0073 + 1.0087)] \times 931.5$ $E_{\text{Lib.}} = 0.0248 \times 931.5 = 23.1012 \text{ MeV} = 3.696 \times 10^{-12} \text{ J}$	1/2
4-1	$\Delta m = [(1.0087 + 235.0439) - (139.9216 + 93.9153 + 2(1.0087))]$ $\Delta m = 0.1983 \text{ u} = 0.1983 \times 1.66 \times 10^{-27} = 3.292 \times 10^{-28} \text{ kg}$	1/2
4-2	$E_{\text{Lib.}} = \Delta m \cdot c^2 = 0.1983 \times 931.5 = 184.72 \text{ MeV} = 184.72 \times 1.66 \times 10^{-13} \text{ J}$ $E_{\text{Lib.}} = 29.56 \times 10^{-12} \text{ J}$	1/2
4-3-1	1 nucleus liberates $29.56 \times 10^{-12} \text{ J}$ N nuclei liberate $63 \times 10^{12} \text{ J}$ $N = 2.131 \times 10^{24}$ nuclei	1/2
4-3-2	The mass lost of $3.292 \times 10^{-28} \text{ kg}$ corresponds to 1 nucleus The mass lost of $\Delta m_{\text{total}}$ corresponds to $2.131 \times 10^{24}$ nuclei Then $\Delta m_{\text{total}} = 0.0007 \text{ kg}$  The mass lost of $3.292 \times 10^{-28} \text{ kg}$ corresponds to 1 nucleus of mass 235.0439 u The mass lost of $0.0007 \text{ kg}$ corresponds to N nuclei of mass $m_t$ Then the mass of the used uranium is: $m_t = 4.99 \times 10^{26} \text{ u} = 0.83 \text{ kg}$ .	1/2  1/2
5-1	For the deuterium nuclei: $3m({}^2_1\text{H}) = 6.0423 \text{ u} = 10.03 \times 10^{-27} \text{ kg}$ gives $36.96 \times 10^{-13} \text{ J}$ $m_2$ gives $4.3 \times 10^7 \text{ J}$ Then we need $m_2 = 4.3 \times 10^7 \times 10.03 \times 10^{-27} / 36.96 \times 10^{-13} = 1.1669 \times 10^{-7} \text{ kg}$  For the uranium nuclei: $m_U = 235.0439 \text{ u} = 3.9 \times 10^{-25} \text{ kg}$ gives $29.56 \times 10^{-12} \text{ J}$ $m_3$ gives $4.3 \times 10^7 \text{ J}$ Then we need $m_3 = 4.3 \times 10^7 \times 3.9 \times 10^{-25} / 29.56 \times 10^{-12} = 5.67 \times 10^{-7} \text{ kg}$	1/2  1/2
5-2	To liberate the same quantity of energy, $4.3 \times 10^7 \text{ J}$ , we need: Fuel: $m_1 = 1 \text{ kg}$ Deuterium nuclei: $m_2 = 1.1669 \times 10^{-7} \text{ kg}$ Uranium nuclei: $m_3 = 5.67 \times 10^{-7} \text{ kg}$ $m_2 < m_3 < m_1$ We prefer using deuterium nuclei.	1/2