

وزارة التربية والتعليم العالي المديرية العامة للتربية دائرة الامتحانات	امتحانات الشهادة المتوسطة	دورة سنة ٢٠٠٤ الإكمالية الاستثنائية
عدد المسائل : سبعة	مسابقة في الرياضيات المدّة: ساعتان	الاسم: الرقم:

**ملاحظة :** يُسمح باستعمال آلة حاسبة غير قابلة للبرمجة أو لاختزان المعلومات أو لرسم البيانات  
يستطيع المرشح الإجابة بالترتيب الذي يناسبه (دون الالتزام بترتيب المسائل الوارد في المسابقة)

### I- (1½ point)

Given the inequality :  $2x + 1 \leq 5(x - 1) + 15$ .

Solve this inequality and represent the solutions on an axis of origin O.

### II- (2 points)

Consider the following numbers A, B and C .

$$A = \frac{1}{5} - \left(\frac{2}{5}\right)^2, \quad B = (2 - \sqrt{5})^2 + 2(8 + \sqrt{20}), \quad C = \frac{-1.25 \times 8 \times 10^7 \times 10^{-4}}{4 \times 10^2} .$$

- 1) Calculate A, B and C showing all the steps of calculation and give each result in its simplest possible form.
- 2) From the numbers A, B and C, choose two opposite numbers and two numbers inverses of each other.

### III-(2½ points)

- 1) Determine the numerical values of a and b so that the numbers 1 and 2 are the roots of the polynomial  $P(x) = ax^2 + bx + 2a - 3b - 9$ .
- 2) Given the polynomial  $Q(x) = (x - 1)(x - 2)$ .
  - a- Show that  $Q(x) - 2 = x(x - 3)$ .
  - b- Solve the equation  $Q(x) = 2$ .

### IV-(3 points)

The opposite circular diagram represents the distribution of marbles in a bag according to their colours :

red : r , green : g , yellow : y , white : w ,  
brown : b.

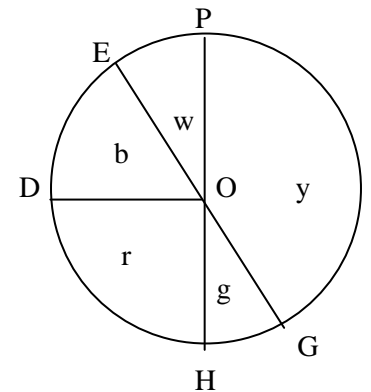
[EG] and [PH] are two diameters of the circle,

$\widehat{DOE} = 60^\circ$  and  $\widehat{DOH} = 90^\circ$ .

- 1) Calculate the angles  $\widehat{EOP}$  ,  $\widehat{POG}$  and  $\widehat{GOH}$ .
- 2) Justify that the yellow colour is the most frequent.
- 3) Knowing that the number of the red marbles is 270, reproduce and complete the following table and verify that the number of marbles in the bag is 1080 :

Colour	r	g	y	w	b
Frequency	270				

- 4) Calculate the percentage of the red marbles.



**V- (3 ½ points)**

ABC is a triangle right angled at A such that  $AB = 4\text{cm}$  and  $AC = 6\text{cm}$ . M is the midpoint of [AC].

- 1) Calculate BM.
- 2) Calculate, rounded to the nearest degree, the angle  $\widehat{ABM}$  and deduce the angle  $\widehat{BMC}$ .
- 3) Let E be the symmetric of B with respect to M.
  - a- Place E and determine the nature of quadrilateral CBAE.
  - b- Calculate the area of CBAE.
- 4) Let G be the symmetric of B with respect to the straight line (AC).
  - a- Place G and determine the nature of quadrilateral GECA.
  - b- Calculate the area of quadrilateral BCEG.

**VI-(2 ½ points)**

Two perpendicular straight lines (d) and (d') intersect in a point O. The circle (C) of center O and radius 4 cuts (d) in A and B. Let M be a point of (C) distinct from A and let L be the midpoint of [AM]. The line (AM) cuts (d') in N.

- 1) Draw a figure.
- 2) a- What is the nature of triangle OLA ? Justify.  
b- Find the locus of L when M moves on the circle (C).
- 3) a- Prove that the two triangles OAN and MAB are similar.  
b- Deduce that the product  $AM \times AN$  remains constant when M moves on circle (C).

**VII-(5 points)**

In an orthonormal system of axes  $x'Ox$ ,  $y'Oy$ , consider the point  $C(0 ; 3)$  and the straight line (D) of equation  $y = \frac{1}{2}x - 2$ .

- 1) (D) cuts  $x'Ox$  in A and  $y'Oy$  in B. Calculate the coordinates of A and B, and draw (D).
- 2) The perpendicular (D') drawn from C to (D) cuts the straight line (D) in I.
  - a- Find the equation of (D').
  - b- Calculate the coordinates of I.
- 3) Let E be the point such that  $\overrightarrow{AE} = \overrightarrow{AB} + \overrightarrow{AC}$ .
  - a- What is the nature of quadrilateral ABEC ?
  - b- Calculate the coordinates of E.
- 4) Let  $M(0 ; m)$  be a point on  $y'Oy$ , where m is a positive number.
  - a- Calculate the numerical value of m such that triangle ABM is right at A.
  - b- For this value of m, the circle of diameter [MB] cuts again the axis  $x'Ox$  in a point H. What are the coordinates of H ? Justify.